Influence of Single Tunnel and Twin Tunnel on Collapse Pattern and Maximum Ground Movement

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Abstract

Particle Flow Code in Two Dimensions (PFC2D) was used in order to examine the influence of single tunnel and twin tunnel on the collapse pattern and maximum ground movement. Since first PFC was calibrated by the experiments, the results obtained were rendered by a uniaxial test. Further, a rectangular model with dimensions of 100 m * 100 m containing both the central tunnel and twin tunnel was built. The center of the single tunnel was placed 25 m under the ground surface, and its diameter changed from 10 m to 35 m with an increment of 5 m. The center of the twin tunnel was situated 25 m under the ground surface, and its diameter was changed from 10 m to 30 m with an increment of 5 m. For measurement of the vertical displacement, one measuring circle with a 2 m diameter was opted on the ground surface above the tunnel roof. The average of the vertical movement of discs covered in these circles was determined as the ground settlement. A confining pressure of 0.01 MPa was applied on the model. The uniaxial compression strength was 0.09 MPa; the results obtained depicted that the tunnel diameter controlled the extension of the collapse zone. Also the vertical displacement at the roof of the tunnel declined by decreasing the tunnel diameter. The ground settlement increased by increasing the tunnel diameter.

Keywords

Tunnel
PFC2D
Settlement

1. Introduction

In the last decade, in Iran, the construction of various tunnels, especially for the transportation purpose, has been required. In some cases where a tunnel must be built next to another tunnel, the construction process must be carried out in such a way that the existing buildings or sub-surface infrastructure are not endangered or damaged. Thus before the designing level, forecasting the probable interaction impacts is vital. It has been predicted that the surface soil settlements (S) in the presence of a single tunnel under a soft soil follow an inverted Gaussian curve, introduced by Peck [1], and investigated by various researchers and measurements (Mair et al., [2]). The introduced equations are as follow:

\[ S = S_{\text{max}} \exp \left( -\frac{x^2}{2\ell^2} \right) \]  \hspace{1cm} (1)

The perpendicular or normal spacing from the centerline axis of the tunnel is shown by \( x \), \( S_{\text{max}} \) is the maximum settlement of the soil surface (upper than the tunnel axis), \( \ell \) is the horizontal settlement, \( V_s \) is the decline of volume, \( V_L \) is the ground loss percentage in the case that soil is uncontactable (\( V_L = V_s/\pi R^2 \)), and \( R \) is the radius of the tunnel. Due to the loss in the tunnel, these settlements are developed. It might be distinguished as the further volume of extracted soil over the volume of final lining. In the process of excavation, the excavated soil in the surrounding of tunnel face is unloaded, and moving inward continues. Due to the nature or properties of the tunnel shield, losses may happen behind the tunnel face. Several site investigations
have proved that Equation 1 is compatible with the green-field sites (Mair et al., [2]); however, in the presence of buildings in cities, this equation is no longer valid. In the case of the tunnels with multiple installations, each settlement is determined by Equation 1 and accumulated. During the installation or construction of each one, the tunnel interaction has been neglected in this equation. It is obvious that construction of tunnels causes the disturbance of soil, which leads to a change in the soil characteristics or it causes the redistribution of the impact of a later tunneling installation in that area. Due to emplacing the new tunnel, the former one and the surrounding soil transfer like a solid structure. The development of “arching” in the surrounding of the new tunnel occurs as the soil stresses are redistributed, and consequently, a sluggish unloading from the tunnel takes place. When a new tunnel is emplaced in the vicinity of the former tunnel, it leads to the distortion and displacement of the first tunnel lining. Based on the position of the soil and its characteristics, the minimum assumed distinct spacing between the tunnels is determined in order to avoid the interaction impacts. When it comes to multiple tunnels, the superposition procedure is proposed, which is according to the Gauss distribution, as follows (Mair et al., [2]):

\[ S = S_{\text{max}(1)} \exp \left( \frac{(x - \bar{x})^2}{2l^2} \right) + \]

\[ S_{\text{max}(2)} \exp \left( \frac{(x - \bar{x})^2}{2l^2} \right) - S_{12} \]

where \( S_{12} = 0 \) for the absence of interaction and \( S \) is the spacing of the tunnels. In the case of ground loss and the diameters of two tunnels being identical, \( S_{\text{max}(1)} = S_{\text{max}(2)} \) and \( l(1) = l(2) \). Totally, the settlement of ground is:

\[ S = S_{\text{max}} \left( \exp \left( \frac{(x - \bar{x})^2}{2l^2} \right) + S_{\text{max}(2)} \exp \left( \frac{(x - \bar{x})^2}{2l^2} \right) \right) \]

Movements of ground caused by single tunneling have been widely studied by several ways such as field observation (e.g. Peck, [1]; Cording and Hansmire, [3]; analytical approach (e.g. Loganathan and Poulos, [4]; Bobet, [5]), numerical modelling (e.g. Rowe et al., [6]; Addenbrooke [7]; Franzius et al. [8]; Zhao [9]; Jain [10]; Thai [11]; Zhang [12]; Li [13]; Ding [14]; Yang [15]; Zheng [16]; Yang [17]; Zhang [18]; Aalianvari [19]), and physical modelling (e.g. Mair [20]; Taylor [21]). Furthermore, investigations of the ground movements caused by multiple tunneling have been carried out. Some researchers have shown that the surface settlement troughs are established by twin tunnels with different forms (e.g. Cording and Hansmire [3]; cooper et al. [22]; Suwansawat and Einstein [23]). In the case of studying the movement associated with multiple tunneling, due to the low-field data investigations generally using numerical modelling (e.g. Addenbrooke [24]; Hunt [25]; Zhou [26]; Zou [27]; Chen [28]; Zhang [29]; Eftekhari [30]; Li [31]; Gao [32]; Li [33]; Sun [34]; Wu [35]; Lee [36]; Wang [37]; Xue [38]; Wang [39,40]) and physical modelling (e.g. Chapman et al. [41,42]; Divall [43]), It is clear that both the numerical and physical modellings give a valuable insight, although due to the intrinsic uncertainties in tunnel engineering, the settlement quantities presented by these investigations can barely represent the real quantities found in an actual condition. In this investigation, the impact of single tunnel and twin tunnel on the collapse pattern and maximum ground movement was examined by Particle Flow Code in Two Dimensions (PFC2D).

2. Particle Flow Code

Particle flow code in two dimensions (PFC2D) is a discreet element code that introduces the substance as a rigid particle assembly that can move discreetly, and its interaction is just at the contacts (Itasca [44]; Potyondy and Cundall [45]). The same as DEM, a central finite difference method has been used in order to calculate the movements and interaction forces of the particles. Both the linear and non-linear contact models with frictional sliding can be used for the contact models. In this investigation, the linear contact model was used. This model established an elastic relationship between the relative displacements and contact forces of particles. Some provided routines were used in order to produce a parallel-bonded particle model for PFC2D (Itasca [44]). To produce this model, some micro-characteristics must be introduced such as parallel-bond stiffness ratio, minimum radius of ball, stiffness ratio of \( k_n \) over \( k_s \), ball-to-ball contact modulus, parallel normal bond strength, coefficient of ball friction, ratio of standard deviation to mean of bond strength in both the normal and shear directions, parallel-bond modulus, parallel shear bond strength, and parallel-bond radius multiplier. A calibration approach is critical in order to establish the suitable micro-characteristics used for the assembly of particles. The tests conducted on the laboratory model specimens cannot directly determine the
particle contact and the bonding properties. The characteristics of the materials that are determined by the laboratory tests are macro-mechanical in nature; this is due to the fact that they show a continuum behavior. A reverse modeling approach was applied in order to determine the suitable micro-mechanical characteristics of the numerical models from the macro-mechanical characteristics defined in the laboratory experiments. The trial-and-error method is one of the approaches that is used to connect these two sets of materials property (Itasca [44]). It includes the assumption of the micro-mechanical property values and comparison of the strength and deformation properties of the numerical models with those of the laboratory specimens. The values of micro-mechanical property that generate a simulated macroscopic result close to that of the laboratory tests are then used to assess the ground settlement.

2.1. Preparation and calibration of numerical model

The uniaxial compression test and the Brazilian test were applied to calibrate the compressive strength, young modulus, and tensile strength of the sample in the PFC2D model. The standard process of generation of a PFC2D assembly to show a test model includes four sections: (a) generation and packing of particles, (b) installation of isotropic stress, (c) deletion of floating particle, and (d) bond installation. Using the micro-characteristics listed in Table 1 and the standard calibration approaches (Potyondy and Cundall [45]), a calibrated PFC particle assembly was provided. The dimensions of the uniaxial model were 54 mm and 108 mm. The sample was created by 12,615 particles. The upper and lower walls were moved toward each other with a low velocity of 0.016 m/s. Figure 1a depicts the contact force chain of the numerical tested sample. The contact force chain is like a cone shape. The stress-strain curve is depicted in Figure 1b. This curve is like a typical experimental stress-strain curve in soil. The uniaxial compression strength and the Young modulus were gained by the stress-strain curve (Table 2). These mechanical characteristics were in a good matching with those of the experimental tests (Table 2). This indicates that the calibration of the model is correct.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type of particle</td>
<td>disc</td>
<td>Stiffness ratio (kn/ks)</td>
<td>2</td>
</tr>
<tr>
<td>Density (kg/m³)</td>
<td>2600</td>
<td>Particle friction coefficient</td>
<td>0.5</td>
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<tr>
<td>Minimum radius (mm)</td>
<td>0.27</td>
<td>Contact bond normal strength, mean (MPa)</td>
<td>0.002</td>
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<tr>
<td>Size ratio</td>
<td>1.56</td>
<td>Contact bond normal strength, SD (MPa)</td>
<td>0.0004</td>
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<tr>
<td>Porosity ratio</td>
<td>0.08</td>
<td>Contact bond shear strength, mean (MPa)</td>
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</tr>
<tr>
<td>Damping coefficient</td>
<td>0.7</td>
<td>Contact bond shear strength, SD (MPa)</td>
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<tr>
<td>Contact young modulus (GPa)</td>
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</table>

**Table 2. Brazilian tensile strength of physical and numerical specimens.**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Experimental test</th>
<th>Numerical simulation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Uniaxial compressive strength (MPa)</td>
<td>0.09</td>
<td>0.092</td>
</tr>
<tr>
<td>Young modulus (GPa)</td>
<td>0.36</td>
<td>0.37</td>
</tr>
</tbody>
</table>

![Figure 1](image1.png)

Figure 1. a) Contact force in numerical model, b) stress-strain curve.
2.2. Preparation of model by PFC

After calibration of PFC2D, a rectangular model including a single tunnel and a twin tunnel was built. The dimensions of the rectangular model were 100 m * 100 m. The diameter of a single tunnel was changed from 10 m to 35 m with an increment of 5 m. The center of the single tunnel was situated 25 m under the ground surface (Figure 2). The diameter of the twin tunnel was changed from 10 m to 30 m with an increment of 5 m. The center of the twin tunnel was situated 25 m under the ground surface (Figure 3). The rectangular model was under a confining pressure of 0.001 MPa. For measurement of the vertical displacement, one measuring circle with a diameter of 2 m was opted on the ground surface above the tunnel roof. The average of the vertical displacement of the discs surrounded in these circles was determined as a ground settlement (Figure 2a and Figure 3a).

![Figure 2. Single tunnel with diameters of a) 10 m, b) 15 m, c) 20 m, d) 25 m, e) 30 m, and f) 35 m.](image-url)
3. Numerical results

3.1. Influence of single tunnel on collapse pattern of numerical model

When the diameter of single tunnel was 10 m (Figure 4), a wedge of particles collapsed inside the tunnel. The size of this wedge was incremented by incrementing the tunnel diameter. The particles of the side-wall of tunnel moved inside the tunnel. It is to be noted that the curvature of the ground surface increase by increasing the tunnel diameter.

Figure 3. Twin tunnel with diameters of a) 10 m, b) 15 m, c) 20 m, d) 25 m, e) 30 m.
Figure 4. Collapse pattern in single tunnel with diameters of a) 10 m, b) 15 m, c) 20 m, d) 25 m, e) 30 m, and f) 35 m.

3.2. Influence of twin tunnel on collapse pattern of numerical model

When the diameter of each tunnel was 10 m (Figure 5), two wedge of particles collapsed inside the tunnel. The size of these wedges was incremented by incrementing the tunnel diameter. The particles of the side-wall of tunnel moved inside the tunnel. It is to be noted that the curvature of ground surface increase by incrementing the tunnels diameter. By comparing Figure 4 and Figure 5, it can be concluded that the volume of the
collapse zone increase by increasing the tunnel number.

3.3. Influence of single tunnel diameter on ground settlement above tunnel roof

Figure 6 depicts the influence of tunnel diameter on the ground settlement above the tunnel roof. The ground settlement was incremented by incrementing the tunnel diameter.

3.4. Influence of twin tunnel diameter on ground settlement above tunnel roof

Figure 7 depicts the influence of the twin tunnel diameter on the ground settlement above the tunnel.
The ground settlement was incremented by incrementing the tunnel diameter. By comparing Figure 6 and Figure 7, it could be concluded that the ground settlement was incremented by incrementing the tunnel number.

3.5. Sensitivity analysis of collapse scope to examine effect of various micro-parameters such as contact bond normal strength, shear bond normal strength, particle friction coefficient, and stiffness ratio (kn/ks) on shape of single tunnel roof collapse

Figure 8 depicts the failure mechanism of tunnel roof with regard to density = 2600 kg/m³, porosity = 0.08, contact young modulus = 1 GPa, and confining pressure = 0.01 MPa. According to Figure 8a, it can be concluded that the widths of the collapse zone tend to decline as the parameter contact bond normal strength increases. Figure 8b depicts that the widths of the collapse zone tend to decline as the parameter contact bond shear strength increases. From Figure 8c and Figure 8d, it is clear that the failure zone is constant with increase in both the particle friction coefficient and the stiffness ratio.

Figure 6. Influence of single tunnel diameter on ground settlement above tunnel roof.

Figure 7. Influence of twin tunnel diameter on ground settlement above tunnel roof.

Figure 8. Influence of various factors on failure mechanisms of single tunnels: (a) Influence of contact bond normal strength on failure mechanisms, (b) Influence of shear bond normal strength on failure mechanisms, (c)
Influence of particle friction coefficient on failure mechanisms, (d) Influences of stiffness ratio (kn/ks) on failure mechanisms.

3.6. Sensitivity analysis of collapse scope to explore influence of different micro-parameters such as contact bond normal strength, shear bond normal strength, particle friction coefficient, and stiffness ratio (kn/ks) on shape of twin tunnel roof collapse

Figure 9 depicts the failure mechanism of the tunnel roof with regard to density = 2600 kg/m³, porosity = 0.08, contact young modulus = 1 GPa, and confining pressure = 0.01 MPa. According to Figure 9a, the widths of the collapse zone tend to decline as the parameter contact bond normal strength increases. Figure 9b depicts that the widths of the collapse zone tend to decline as the parameter contact bond shear strength increases. From Figure 9c and Figure 9d, it is clear that the failure zone is constant by increasing both the particle friction coefficient and the stiffness ratio.

Figure 9. Influence of various factors on failure mechanisms of single tunnels: (a) Influence of contact bond normal strength on failure mechanisms, (b) Influence of shear bond normal strength on failure mechanisms, (c) Influence of particle friction coefficient on failure mechanisms, (d) Influence of stiffness ratio (kn/ks) on failure mechanisms.

4. Conclusions

In this investigation, the influence of single tunnel and twin tunnel on the collapse pattern and maximum ground movement was examined by particle flow code in two dimensions (PFC2D). Since first PFC was calibrated by the experiments, the test results were rendered by the uniaxial test. Further, a rectangular model with dimensions of 10 m * 10 m containing both the central tunnel and the twin tunnel was built. The center of single tunnel was placed 25 m under the ground surface, and its diameter was changed from 10 m to 35 m with an increment of 5 m. The center of the twin tunnel was placed 25 m under the ground surface, and their diameters were changed from 10 m to 30 m with an increment of 5 m. A confining pressure of 0.01 MPa was applied to the model. The results obtained showed that:

- The volume of the collapsed wedge was incremented by incrementing the tunnel diameter.
The volume of the collapsed wedge was incremented by incrementing the tunnel number.

The ground settlement was incremented by incrementing the tunnel diameter.

The ground settlement was incremented by incrementing the tunnel number.

The widths of the collapse zone tend to decline as the parameter contact bond normal strength increases.

The widths of the collapse zone tend to decline as the parameter contact bond shear strength increases.

The failure zone was constant by increasing both the particle friction coefficient and the stiffness ratio.

The failure zone volume was incremented by increasing the tunnel diameter.

The failure zone volume was incremented by increasing the tunnel number.

References


تاثیر تونل‌های تک گانه و دو گانه بر الگوی ریزش و نشست سطح زمین

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چکیده:

به منظور بررسی تاثیر تونل‌های تک گانه و دو گانه بر الگوی ریزش و بیشینه جابجایی سطح زمین، از کد جریان ذره استفاده شد در مرحله اول، نرم افزار PFC با نتایج تک محوره خصوصاً آزمایشگاهی کامپیوتر کرده‌اید در مرحله دوم مدل‌پیمایی عمدی با ابعاد 100 m × 100 m حاوی یک تونل و دو تونل ساخته شد. مرکز تونل‌ها 25 m زیر سطح زمین قرار گرفت. قطر تونل تک گانه از 10 m تا 10 m × 25 m با گام 5 m متغیر است. قطر تونل دو گانه از 10 m تا 20 m با گام 5 m متغیر است. در سطح زمین بالای تونل نصب شد میانگین جابجایی عمدی دوکسرهای موجود در اندازه گیری جابجایی عمودی، یک دایره طراحی گیر جابجایی با قطر 2 m در سطح زمین بالای تونل نصب شد. نتایج نشان می‌دهد که قطر تونل کننده وسعت ناحیه آوار است و همچنین جابجایی ارتفاع تونل با کاهش قطر تونل، کاهش می‌یابد. نشست زمین با افزایش قطر تونل زیاد می‌شود.

کلمات کلیدی: تونل، PFC2D، نشست.