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## A finite element model to simulate magnetic field distribution and laboratory studies in wet low-intensity magnetic separator

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Keywords	Abstract
	Low-intensity magnetic separators are widely used in the research works and the
Magnetic Separation	industry. Advancement in the magnetic separation techniques has led to an expansion in
	the application of this method in different fields such as enrichment of magnetic
Wet Drum Magnetic	mineral, wastewater treatment, and medicine transfer in the human body. In the mineral
Separator	processing industry, the main application of wet magnetic separation is via drum
	separators. The design of this separator is based on drum rotation inside a tank media,
Magnetic Field	where a permanent magnet placed inside the drum as an angle form produces a magnetic
Simulation	field. In the present work, the magnetic variables involved (magnetic flux density,
	intensity of magnetic field, and gradient of magnetic field intensity) were simulated in
Finite Element Method	the drum wet low-intensity magnetic separator using the finite element method and a COMSOL Multiphysics simulator; these variables were further validated through the
	measured data. A comparison between the simulation and laboratory measurements (of
	the magnetic field) showed that the mean value of the simulation error in 94 points in 2
	sections was equal to 9.6%. Furthermore, the maximum simulation error in the middle
	of the magnets, as the most important part of the magnetic field distribution in the
	process of magnetic separation, was in the 6th direction and equal to 7.8%. Therefore,
	the performed simulation can be applied as a first step to design and construct more
	advanced magnetics separators.

#### 1. Introduction

The demand for effective, clean, and simple separation techniques is increasing, while declining mineral resources and environmental restrictions have become more stringent. Since magnetic separation is clean and proceeds at numerous conditions, it has been preferred over other separation techniques in many situations [1], and has led to its unique position among the separation technologies.

Magnetic separations have, for decades, been applicable processes in different industries from production ranging steel to coal desulfurization [2]. Magnetic separation has been used for separation of gangue from ore to enrich low-grade ores [3-8], separation of magnetic from non-magnetic waste [9, 10], heavy media separation [11], separation of pyrite ( $FeS_2$ ) from coal for desulfurization [2], kaolin (clay) decolorization and removing ironic impurities [2, 12], processing a rare earth mineral deposit [13, 14], water treatment and metal removal [2], waste water treatment [15], food industry and removing rare earth elements [2], etc. Furthermore, in the field of biotechnology such as protein and DNA purification, cell separation, separation of biological cells and drug delivery [2, 10, 16], and biocatalysis and diagnostics, magnetic separation has had a wide range of usage.

According to the different parameters (consisting of intensity of magnetic field, its gradient, and dry or wet operation of the equipment), magnetic separators have been classified as drv

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low-intensity magnetic separators, wet low-intensity magnetic separators, dry high-intensity magnetic separators, wet high-intensity high-gradient magnetic separators, and finally. Eddy-current separators and separation in a magnetic fluid [17]. In another classification, the magnetic separation equipment for mineral processing generally falls into three medium-, categories: low-, basic and high-intensity, based on the relative magnetic field strength employed to accomplish separation [18]. By far, the most frequently used wet low-intensity magnetic separators are drum separators [9, 19]. These separators are used mainly for concentration of strongly magnetic ores (such as magnetite) and recovery of the heavy media (such as magnetite or ferrosilicon) used in dense medium separation [9, 19, 20]. It is probably true to say that the magnets are the heart of the wet drum magnetic separators. In terms of wet drum magnetic separators, the permanent magnets installed inside the drum generate an external magnetic field of a strength that is dependent on the intensity of the magnets. Most wet drum magnetic separators are of the type with ceramic ferrite magnets generating a field strength between 1500 and 2500 gauss [20].

The magnetic separation process has been simulated in limited devices. The majority of these simulations are related to the HGMS equipment and using the CFD numerical method [1, 21-27]. This is while only one simulation study was conducted for the wet LIMS device. In the mentioned study, the flow of materials in the LIMS device was simulated using a combination of the FEM and CFD numerical methods [28].

The first step in simulating the magnetic separation process is to simulate the magnetic field and the corresponding variables. The most accurate numerical method for simulating magnetic variables is the finite element numerical method (FEM) [29-33]. There are several available FEM-based simulators such as COMSOL Multiphysics, Opera, Faraday, and EMAG, which can be successfully used to calculate the magnetic field parameters [28].

In this work, a laboratory wet low-intensity magnetic separator (LIMS) device was primarily disassembled. Next, through the use of the reverse engineering process, the mechanical and magnetic information of the magnets inside the drum was extracted. The magnetic variables of magnetic flux density (B) and magnetic field intensity (H) were then simulated using the finite element method (FEM) and a COMSOL Multiphysics simulator. In the next step, the gradient of magnetic field intensity ( $\nabla$ H) was generated via the Helmholtz math model in the COMSOL Multiphysics simulator. Ultimately, the results of the simulation and laboratory measurements (of the magnetic field) were compared so as to validate the results of the simulation.

#### 2. Material and methods

# 2.1. Separator device and measuring instrument

In the present work, a wet low magnetic separator device (BOXMAG-Rapid Limited model) was used to simulate the magnetic variables involved in a wet low-intensity magnetic separator. This device contains three main parts, namely a magnetic cylinder, a magnetic sector (consisting of permanent magnets placed in the cylinder in angle form), and a tank (the main position of magnetic separation). It is of note that in the device, magnets are placed in an axial arrangement. Besides, the magnetic sector is comprised of three ferrite types (ceramic rectangular cube block magnets with similar upper and bottom magnets). Figure 1 shows the magnetic separator device, magnets, and 3D initial model. The cylindrical drum and separator tank are steel (316). The remnant magnetization (with the Gaussian unit, a characteristic of the permanent magnet) of all three magnets was 1,500 gauss. The magnetic field values were measured using a gauss-meter (F.W. Bell (SYPRIS), Model 5170) around the magnetic sector of the device at different distances and directions.

### 2.2. Simulation method and modeling theory

The maps of the magnetic sector, magnetic cylinder, and tank were prepared in the SolidWorks software. Simulation of the magnetic variables was performed through FEM numerical modeling in the COMSOL Multiphysics simulator by the AC/DC module and the Magnetic Fields, No Current options.

In a magnetic separator, when a particle is exposed to an external magnetic field (resulting from the arrangement of permanent magnets), the magnetic force applied to the magnetic field is the main force input in the particle, which is in opposition to the gravity and drag forces [20, 34-36]. The magnetic force applied to the particles carried by the fluid flow (in the magnetic field of the permanent magnet) is a function of the particle magnetization and the gradient of the magnetic field, calculated by Eq. 1.

$$\overline{F_M} = \mu_0 V_m M \,\nabla H \tag{1}$$

where  $\mu_0$  is the permeability magnetic coefficient in a vacuum ( $4\pi \times 10^{-7}$  Tm/A), Vm is the volume of particles, M is the magnetization with Am<sup>-1</sup> unit, H is the intensity of magnetic field, and finally, ( $\nabla H$ ) is the gradient of magnetic field intensity [24, 28, 36].

Therefore, the gradient of the magnetic field should be determined in order to calculate the magnetic force. In a COMSOL Multiphysics simulator, the AC/DC module and the Magnetic Fields, No Current options, are used to simulate the magnetic variables of permanent magnets. In this method, the basic equations used for solving the magnetic field are based on Eqs. 2 and 3 [37]:

$$\nabla_{\cdot} \left( \mu_0 \mu_r H \right) = 0 \tag{2}$$

$$H = -\nabla V_m + H_b \tag{3}$$

After calculating the value of magnetic field intensity in different detections, the gradient of magnetic field intensity was quantitatively calculated in the x, y, and z-directions and different points. The gradient of the magnetic field intensity was calculated via Eq. 4. These calculations were performed in the COMSOL Multiphysics simulator using the Helmholtz mathematical model [37].

$$\nabla \mathbf{H} = \left( \frac{\partial}{\partial \mathbf{x}}, \frac{\partial}{\partial \mathbf{y}}, \frac{\partial}{\partial \mathbf{z}} \right) \left( \mathbf{H}_{\mathbf{x}}, \mathbf{H}_{\mathbf{y}}, \mathbf{H}_{\mathbf{z}} \right)$$

$$\nabla \mathbf{H} = \begin{bmatrix} \frac{\partial \mathbf{H}_{\mathbf{x}}}{\partial \mathbf{x}} & \frac{\partial \mathbf{H}_{\mathbf{x}}}{\partial \mathbf{y}} & \frac{\partial \mathbf{H}_{\mathbf{x}}}{\partial \mathbf{z}} \\ \frac{\partial \mathbf{H}_{\mathbf{y}}}{\partial \mathbf{x}} & \frac{\partial \mathbf{H}_{\mathbf{y}}}{\partial \mathbf{y}} & \frac{\partial \mathbf{H}_{\mathbf{y}}}{\partial \mathbf{z}} \\ \frac{\partial \mathbf{H}_{z}}{\partial \mathbf{x}} & \frac{\partial \mathbf{H}_{z}}{\partial \mathbf{y}} & \frac{\partial \mathbf{H}_{z}}{\partial \mathbf{z}} \end{bmatrix} = \begin{bmatrix} \mathbf{H}_{\mathbf{xx}} & \mathbf{H}_{\mathbf{xy}} & \mathbf{H}_{\mathbf{xz}} \\ \mathbf{H}_{\mathbf{yx}} & \mathbf{H}_{\mathbf{yy}} & \mathbf{H}_{\mathbf{yz}} \\ \mathbf{H}_{zx} & \mathbf{H}_{zy} & \mathbf{H}_{zz} \end{bmatrix}$$

$$\nabla \mathbf{H}_{\mathbf{x}} = \mathbf{H}_{\mathbf{xx}} + \mathbf{H}_{\mathbf{yx}} + \mathbf{H}_{zx}$$

$$\nabla \mathbf{H}_{\mathbf{y}} = \mathbf{H}_{\mathbf{xy}} + \mathbf{H}_{\mathbf{yy}} + \mathbf{H}_{zy}$$

$$\nabla \mathbf{H}_{z} = \mathbf{H}_{\mathbf{xz}} + \mathbf{H}_{\mathbf{yz}} + \mathbf{H}_{zz}$$

$$(4)$$

#### 3. Simulation steps

In order to simulate the magnetic variables in the COMSOL Multiphysics, the steps mentioned in Figure 2 were followed.



Figure 1. Schematic representation of the wet LIMS device (A), initial 3D model (B), and magnets (C).



Figure 2. Flow diagram of the simulation steps of magnetic variables in COMSOL Multiphysics.

The following steps are discussed in details in the following sections.

# **3.1.** Determining physics, materials, and geometry criteria

In order to simulate the magnetic field resulting from permanent magnet in COMSOL Multiphysics, the AC/DC module, and the Magnetic Fields, No Current option, was used. In the considered problem, there exist three elements, namely ferrite (ceramic) cuboid magnets, steel cylindrical drum and separator tank (steel 316), and the air covering the magnets. To simulate the magnetic field further employed, were three block-shaped magnets with certain dimensions and arrangements, a steel cylindrical drum (with magnets mounted on the inner shaft), and a separator tank. Figure 3 shows a schematic view of the geometry created in the simulator, COMSOL Multiphysics.



Figure 3. Schematic view of the created geometry of the wet LIMS in the COMSOL Multiphysics (dimension is based on the meter).

#### 3.2. Boundary conditions

In this step, the region related to the generation of the magnetic field was to be specified. The generation power of the magnetic field was also determined using the remnant magnetization variable (1,500 gauss for each one of the three magnets). This value should be applied in a particular direction, referred to as the polarization direction, and determined by the N and S poles of the magnets. In the desired problem, this direction was determined after determining the N and S poles of the magnets and the angle of the magnets with the horizon (X-axis) (Figure 4). Moreover, the magnetic insulation boundary condition was considered as surrounding cubic plates, which limited the calculation of the magnetic field in this space.



Figure 4. Position of the poles (N and S) in the magnets of the wet LIMS.

#### 3.3. Mesh generation

In general, to create a mesh in the COMSOL simulator, a certain amount of each element is determined by considering the type of the physics. It is possible to use a finer mesh element to reach a higher precision or to reduce the computational size by adopting a larger mesh size. Figure 5 illustrates a view of the constructed mesh where the inlet of the separator is located on the left, and the rotating cylinder shell of the separator is further characterized by a blue circular dense mesh. In this figure, the position of the magnets is also determined and their colored spectrum, according to the legend, indicates the distribution of the magnetic flux density in the space around the magnets. The most important point is that triangular meshes are used so as to achieve a better convergence and stability in the solution.



Figure 5. Schematic view of the created mesh with the magnetic flux density distribution in the device.

#### 4. Results and discussion

#### 4.1. Simulation of magnetic flux density (B)

After solving the physics of the problem, the graphical results of the magnetic flux density were shown in Figure 6. As observed, the magnetic flux density value on the magnet was 900 to 1000 gauss, considering the legend on the right side of the figure.

#### 4.2. Simulation of magnetic field intensity (H)

Given that the main purpose of the simulation is to determine H and the gradient of magnetic field intensity, Figures 7, 8, and 9 indicate the values for the magnetic field intensity in the x, y, and z directions.

In addition to the graphical results (Figures 6, 7, and 8), the values (Hx, Hy, Hz) for the various coordinates (x, y, z) are also quantitatively available. Following the calculation of H in various directions, the gradient of the magnetic field intensity was further calculated in different directions (x, y, z) using the Helmholtz model by the COMSOL Multiphysics simulator.



Figure 6. Schematic view of magnetic flux density (Tesla) around the permanent magnets (cylinder and separator tank).



Figure 7. Changes in the magnetic field intensity value in the x-direction (Hx) in wet LIMS device.



Figure 8. Changes in the magnetic field intensity value in the y-direction (Hy) in wet LIMS device.



Figure 9. Changes in the magnetic field intensity value in the z-direction (Hz) in the y-z plane in wet LIMS.

# 4.3. Validation of simulation results of magnetic field

In order to validate the simulation results of the magnetic field, the size of the magnetic field (in Gauss) was measured at 94 points around the magnetic sector using a gauss-meter. Of these, we selected 49 points in the middle section of the magnets and 45 points in the edges of the magnets in 6 directions with different angles and different distances from the magnets (Figure 10). The quantitative comparison of the measured and simulated magnetic field intensity at different points (six different directions at different intervals from the surface of the cylinder shell) is

shown in Figure 11 (6 directions and the middle section of the magnet) and Figure 12 (6 directions and edges of the magnets).

As it can be seen in Figure 11, the value for the magnetic field intensity was reduced by an increase in the distance from the cylinder surface, a trend observable in both the laboratory measurement and the results of the simulation. On the other hand, the results of the magnetic field simulation were in agreement with those of laboratory measurement and simulation were further compared on the edge of the magnets (Figure 12). In general, the evaluation of Figures11 and 12

showed that the quantitative results of the magnetic field simulation were consistent with the laboratory measurements.

In order to investigate the quantitative adaptability of laboratory measurements and simulation results of magnetic field magnitude, the R squared values of the experimental and simulation curves were separately measured in 6 directions at different distances from the drum surface, and were further added to Figures11 and 12, where the minimum values of R squared for experimental and simulation curves were 0.97 and 0.96, respectively, indicating the high compliance of the laboratory and simulation values.



Figure 10. Schematic view of the middle section and the edge of magnets along with directions and selected angles to measure the magnetic field magnitude.



Figure 11. Measured and simulated values of magnetic field magnitude (gauss) in 6 directions and different distances from the surface of the drum in the middle section of the magnets.



Figure 12. Measured and simulated values of magnetic field magnitude (gauss) in 6 directions and different distances from the surface of the drum at the edge of the magnets.

It is to be noted that the effective magnetic field in the surface of the drum shell and in the middle section of the magnets was about 1,000 gauss (based on the simulation and measurement results, Figure 11), which was slightly higher at the edge of the magnets, about 1100 gauss (Figure 12). This helps increasing the weight recovery of magnetic materials and reduce the waste of magnetic materials in the tailings. Although in the normal mode, the arrangement of the magnets is symmetrically placed inside the cylinder, in certain magnetic separation devices, it is possible to move the magnetic field toward the feed inlet or the outlet of the concentrate. Given the magnitude of the magnetic field, it is clear that if the magnets move towards the feed inlet, the magnitude of the magnetic force applied to the particles increases as a result of an increase in the effective magnetic field intensity, thereby increasing the weight recovery of the product concentrate. Moreover, if the angle of the magnets moves towards the concentrate output, the amount of magnetic force applied to the particles decreases as a result of the effective reduction in the effective magnetic field, hence an increase in the grade of the product of the concentrate.

#### 5. Conclusions

In the present research work, the magnetic variables of the magnetic flux density, intensity of magnetic field, and gradient of the magnetic field intensity were simulated in a drum wet low-intensity magnetic separator using the finite

element method (FEM) and employing a COMSOL Multiphysics simulator. Since the magnetic field of the LIMS device is produced with permanent magnets placed inside the drum as an angle form, the AC/DC module and the Magnetic Fields, No Current modeling option in COMSOL Multiphysics were used to simulate the magnetic variables including the magnetic flux density, magnetic field intensity, and gradient of magnetic field intensity. The preliminary simulation results showed that the value of the magnetic flux density on the magnet ranged from 900 to 1000 gauss, and the value of the magnetic field intensity was reduced by an increase in the distance from the cylinder surface. This decreasing trend was obvious in both the laboratory measurement and the results of the simulation. In order to quantitatively validate the simulation results of the magnetic field, the size of the magnetic field was measured at 94 points around the magnetic sector in the middle and at the edge of the magnets. The comparison of the simulation and laboratory measurements showed that the mean value for the simulation error was equal to 9.6%. Moreover, the minimum values of R squared for the experimental and simulation curves were 0.97 and 0.96, respectively, indicating the high compliance of the laboratory and simulations values. Therefore, the performed simulation can be the first step in designing and constructing more developed magnetic separators with higher efficiencies.

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# شبیهسازی توزیع میدان مغناطیسی با استفاده از روش مدلسازی المان محدود و مطالعات آزمایشگاهی در جداکننده مغناطیسی شدت پایین تر

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#### چکیدہ:

جداکنندههای مغناطیسی شدت پایین به طور گستردهای در تحقیقات و صنعت استفاده میشوند. پیشرفت در تکنیکهای جداسازی مغناطیسی منجر به گسترش استفاده از این روش در زمینههای مختلف مانند فرآوری مواد معدنی مغناطیسی، تصفیه فاضلاب و انتقال دارو در بدن انسان شده است. در صنعت فرآوری مواد معدنی، کاربرد اصلی جدایش مغناطیسی تر از طریق استفاده از جداکنندههای مغناطیسی استوانهای امکانپذیر میباشد. طراحی این جداکننده بر اساس چرخش استوانه در داخل یک مخزن میباشد، به گونهای که مجموعهای از آهنرباهای دائمی به شکل زاویهای درون استوانه قرار گرفته (قطع مغناطیسی) و یک میدان مغناطیسی تولید می کنند. در این پژوهش، متغیرهای مغناطیسی شامل (چگالی شار مغناطیسی، شدت میدان مغناطیسی و گرادیان شدت میدان مغناطیسی) در مغناطیسی تولید میکنند. در این پژوهش، متغیرهای مغناطیسی شامل (چگالی شار مغناطیسی، شدت میدان مغناطیسی و گرادیان شدت میدان مغناطیسی) در جداکننده مغناطیسی شدت پایین تر آزمایشگاهی با استفاده از روش عددی المان محدود و شبیه از مین مناطیسی و گرادیان شدت میدان مغناطیسی) در ادامه متغیرهای شبیه ازی شد و این پژوهش، متغیرهای مناطیسی شامل (چگالی شار مغناطیسی، شدت میدان مغناطیسی و گرادیان شدت میدان مغناطیسی ادر میدان مغناطیسی از مین تر آزمایشگاهی با استفاده از روش عددی المان محدود و شبیه از مین منایم سین در است. حرو است، در ادامه متغیرهای شبیه ازی شده از طریق اندازه گیریهای آزمایشگاهی اعتبار سنجی شده است. مقایسه بین نتایج شبیه سازی و اندازه گیری های آزمایشگاهی (میدان مغناطیسی) نشان داد که میانگین مقدار خطای شبیه سازی در ۹۴ نقطه در ۲ مقطع اندازه گیری برابر با ۹/۹٪ بوده است. علاوه بر این، حداکثر خط ای شبیه سازی در مقطع وسطی آهنرباهای دائمی موجود در استوانه دستگاه جداکننده، به عنوان مهم ترین بخش تولید میدان مغناطیسی در فرآیند جداسازی مغناطیسی، در راستای ششم اندازه گیریها و برابر ۸/۹٪ بوده است؛ بنابراین، شبیه سازی انجام شده می تواند به عنوان نخستین گام برای طراحی و ساخت

**کلمات کلیدی:** جدایش مغناطیسی، جداکننده مغناطیسی استوانهای تر، شبیهسازی میدان مغناطیسی، روش المان محدود.